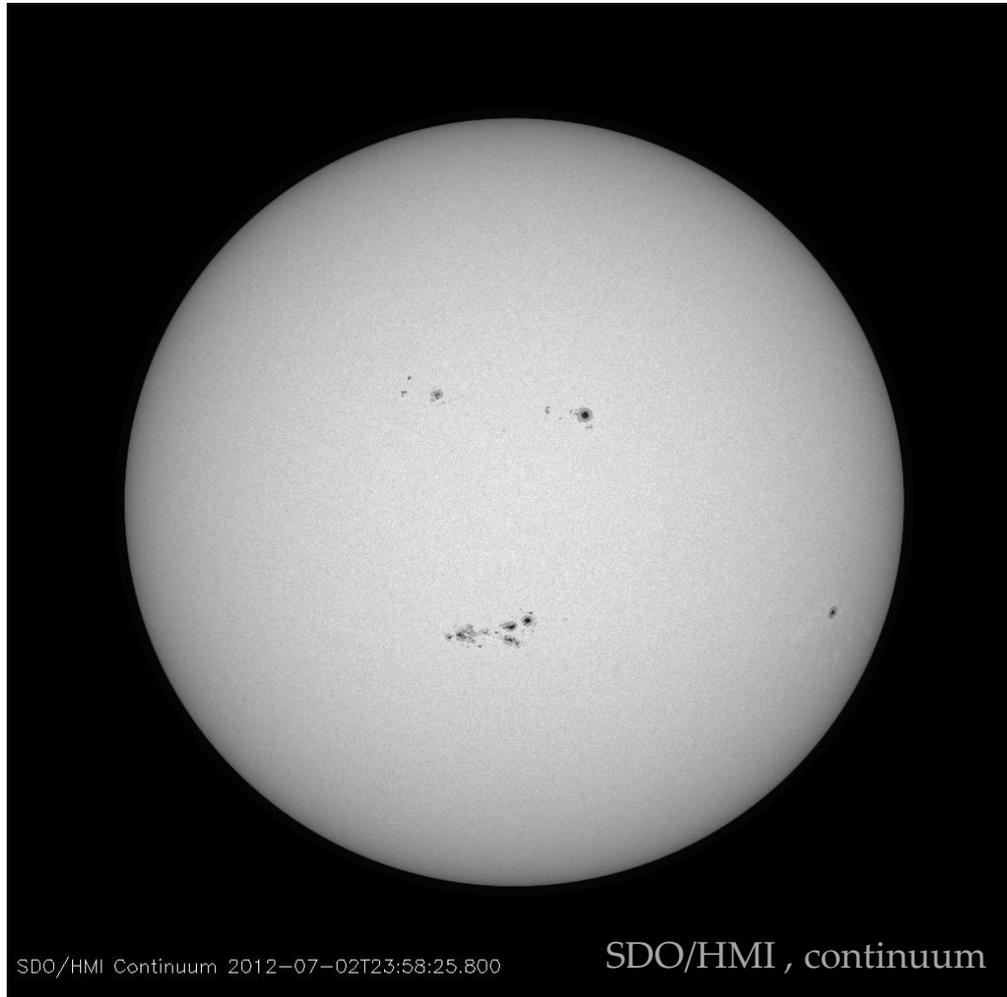


# Using Observations to Understand the Causes of Space Weather

Aenny Malanushenko (HAO)

# The Sun: *in visible light*

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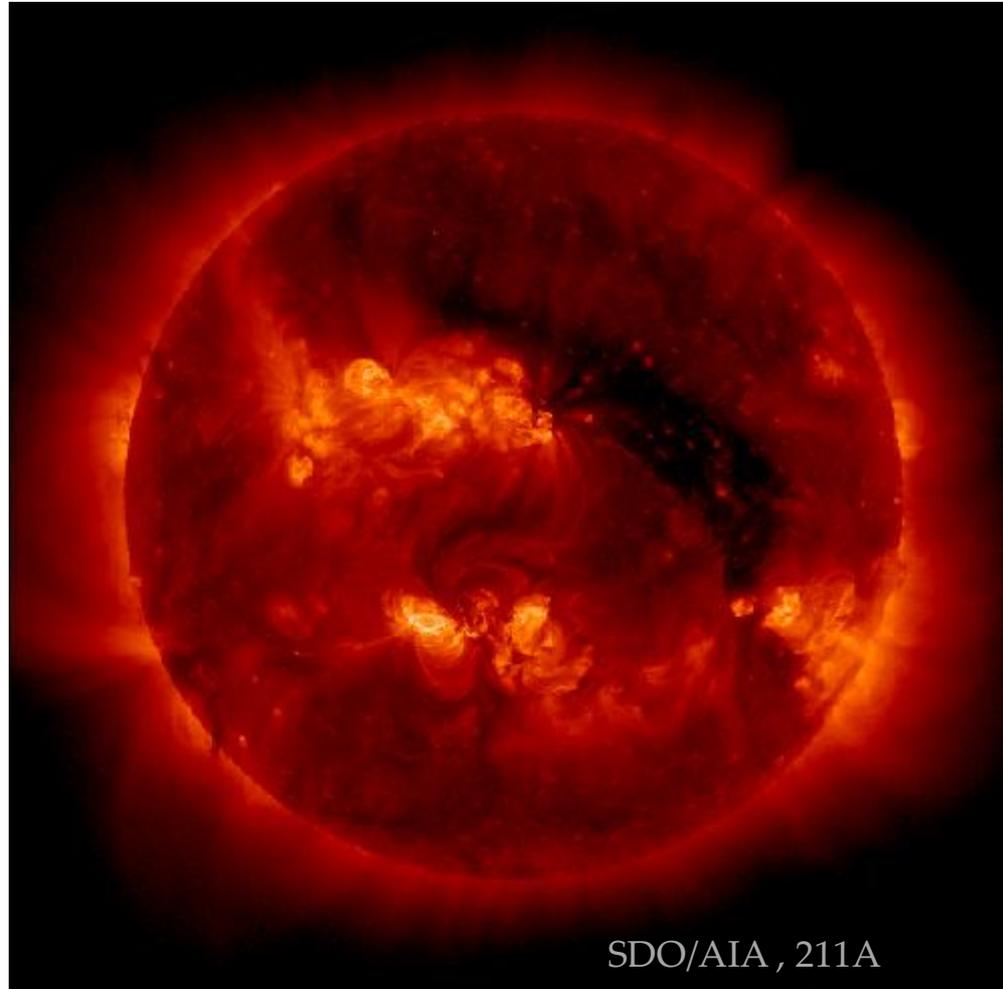


SDO/HMI Continuum 2012-07-02T23:58:25.800

SDO/HMI, continuum

# The Sun: in Extreme Ultraviolet

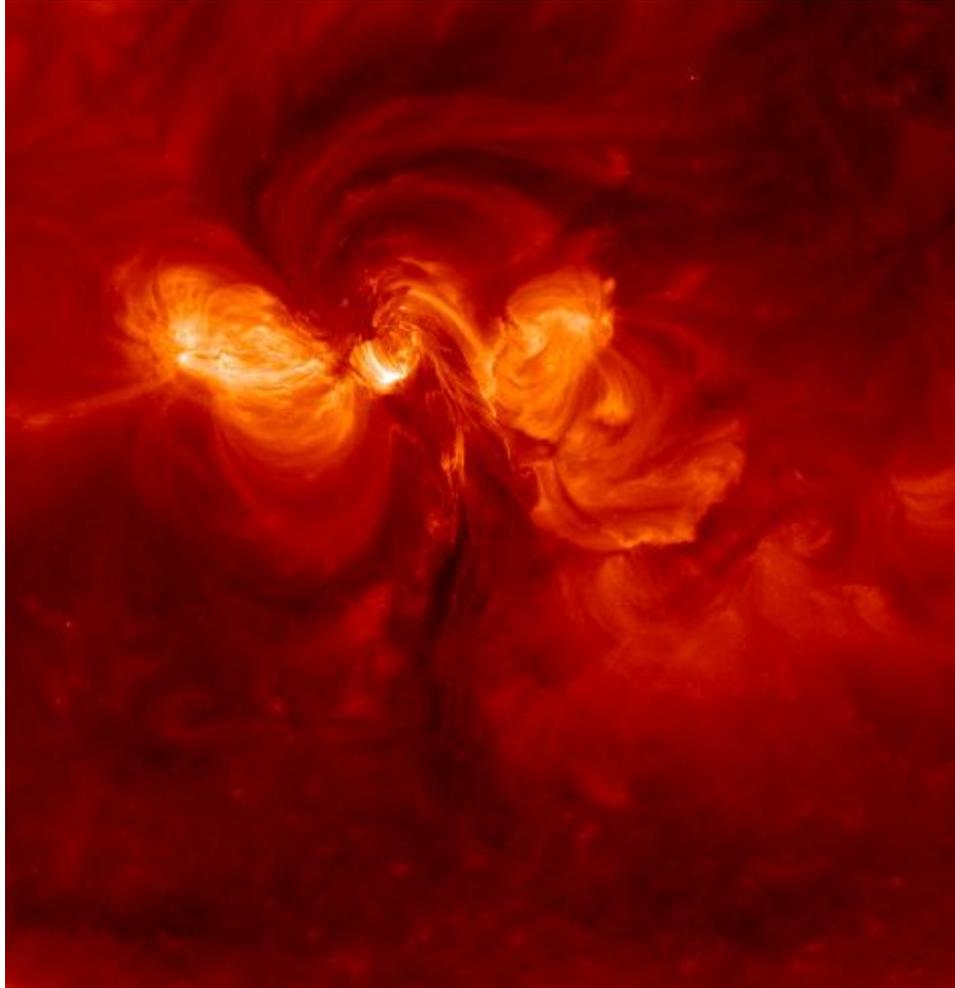
---



SDO/AIA, 211A

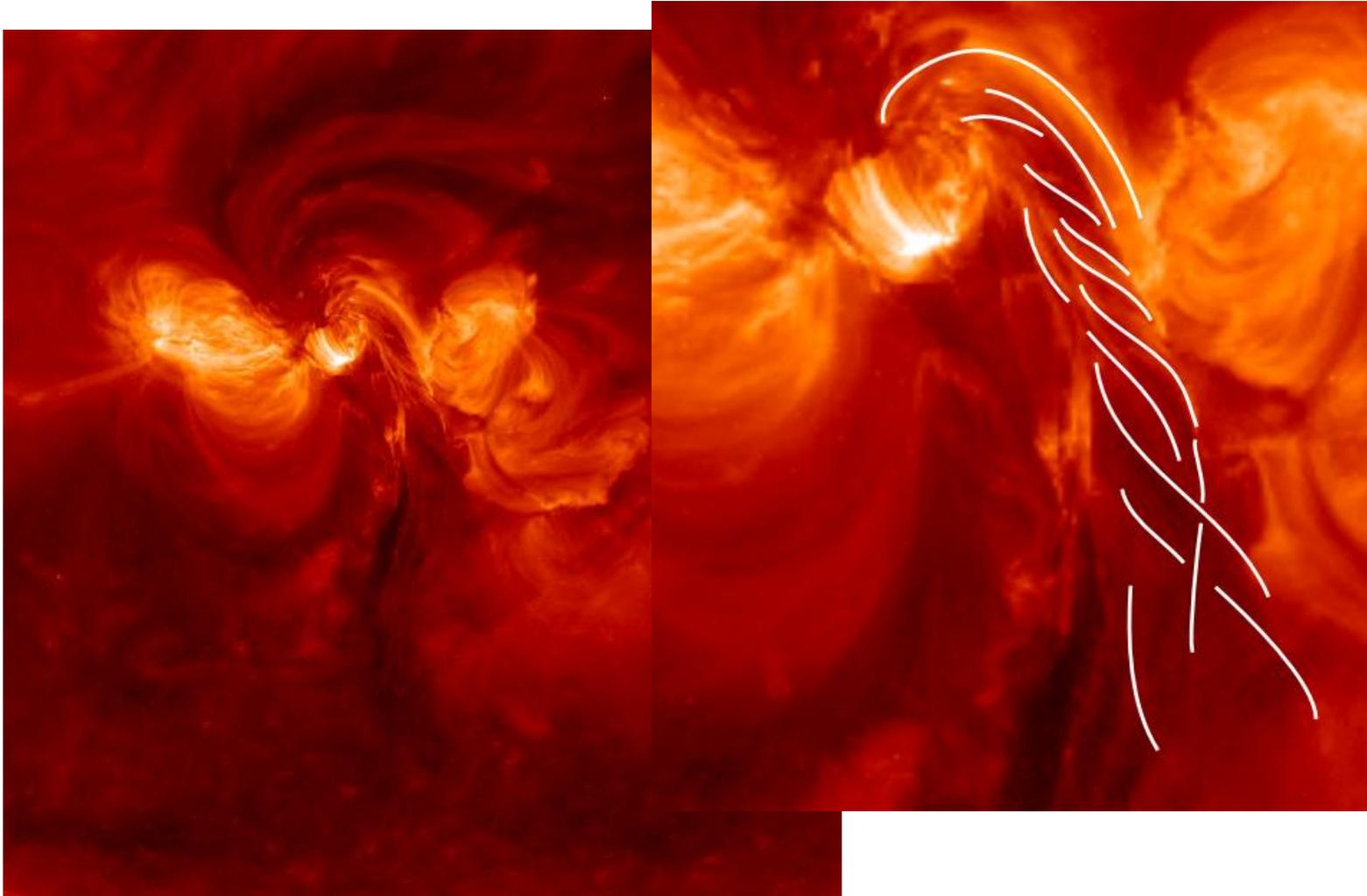
# The Sun: *Eruptive Activity*

---



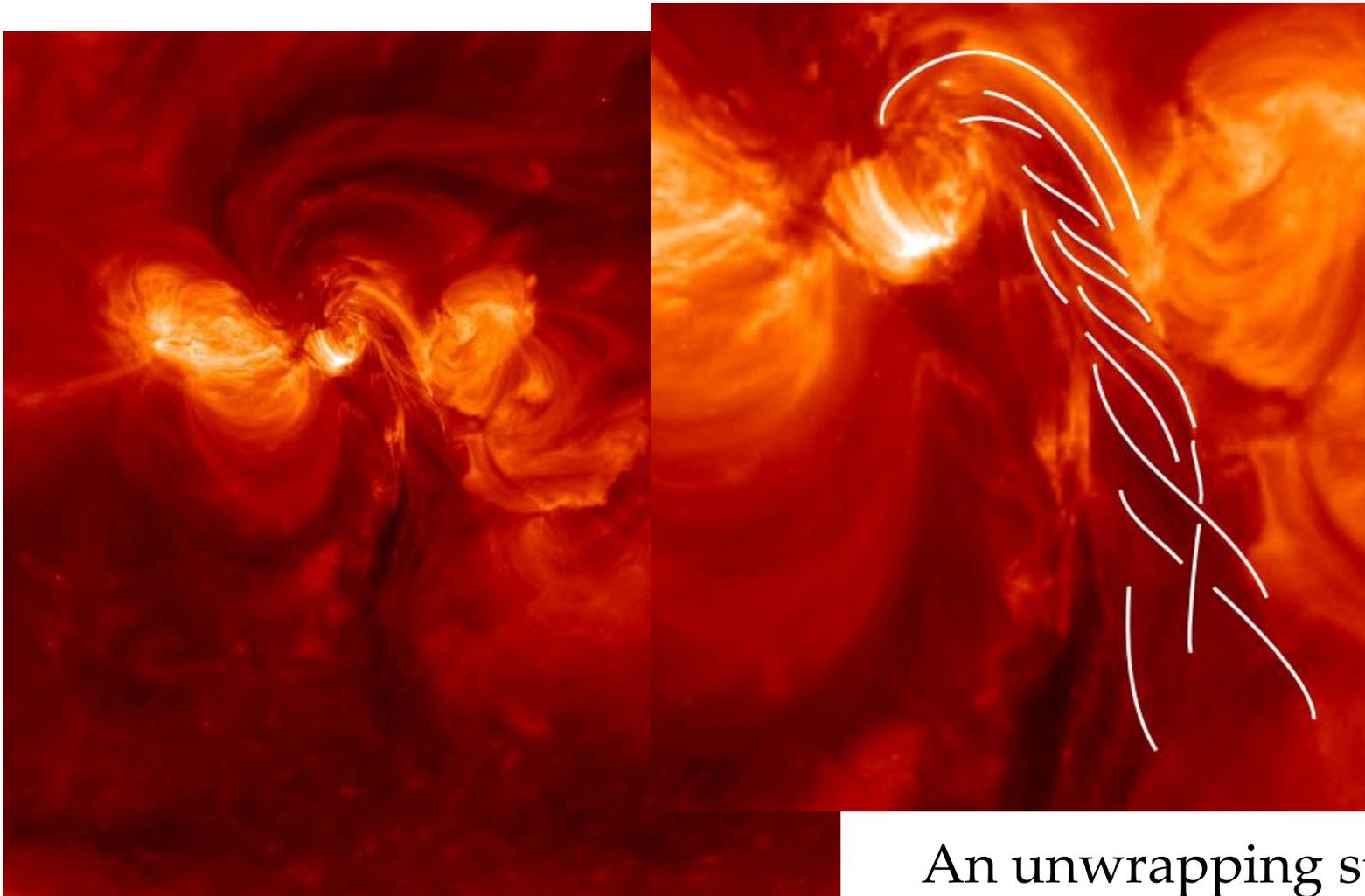
# The Sun: *Eruptive Activity*

---



# The Sun: *Eruptive Activity*

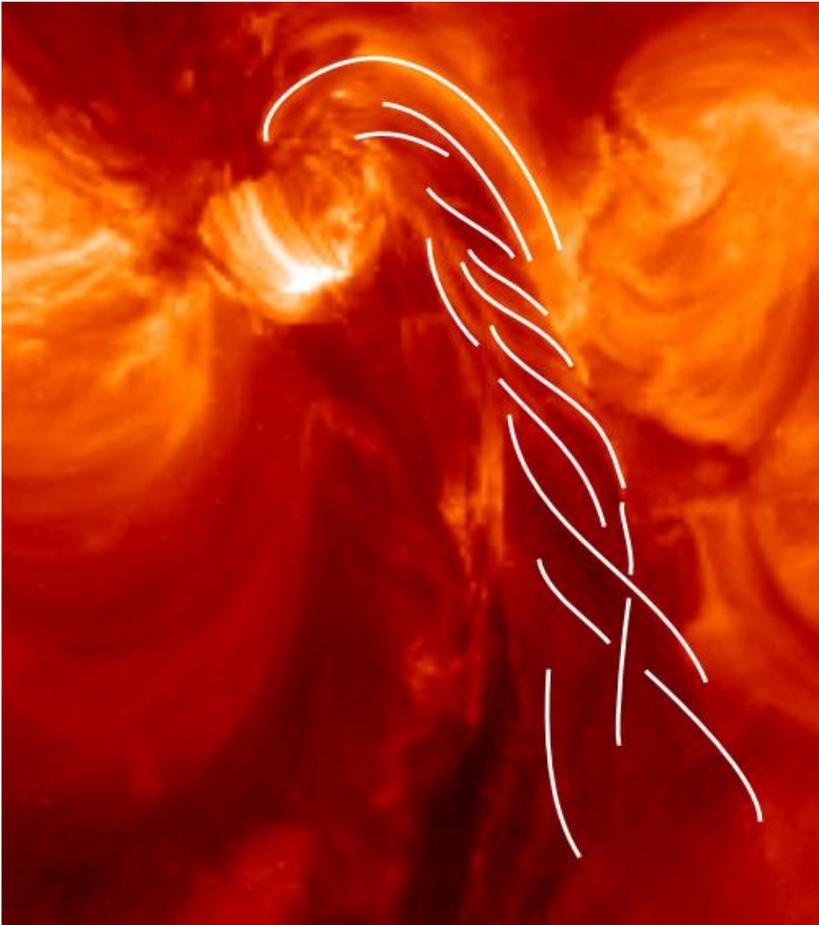
---



An unwrapping structure!

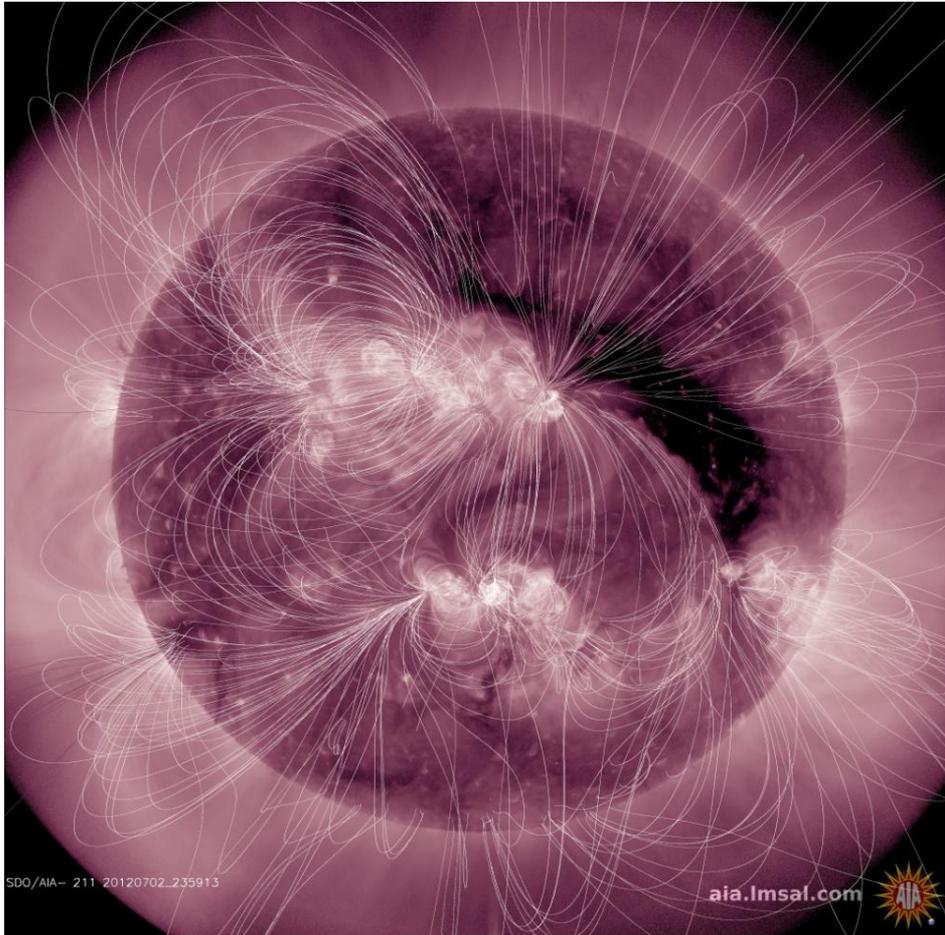
# An unwrapping structure! but what exactly is “unwrapping”?

---



Short answer:  
magnetic field lines.

# An unwrapping structure! but what exactly is “unwrapping”?

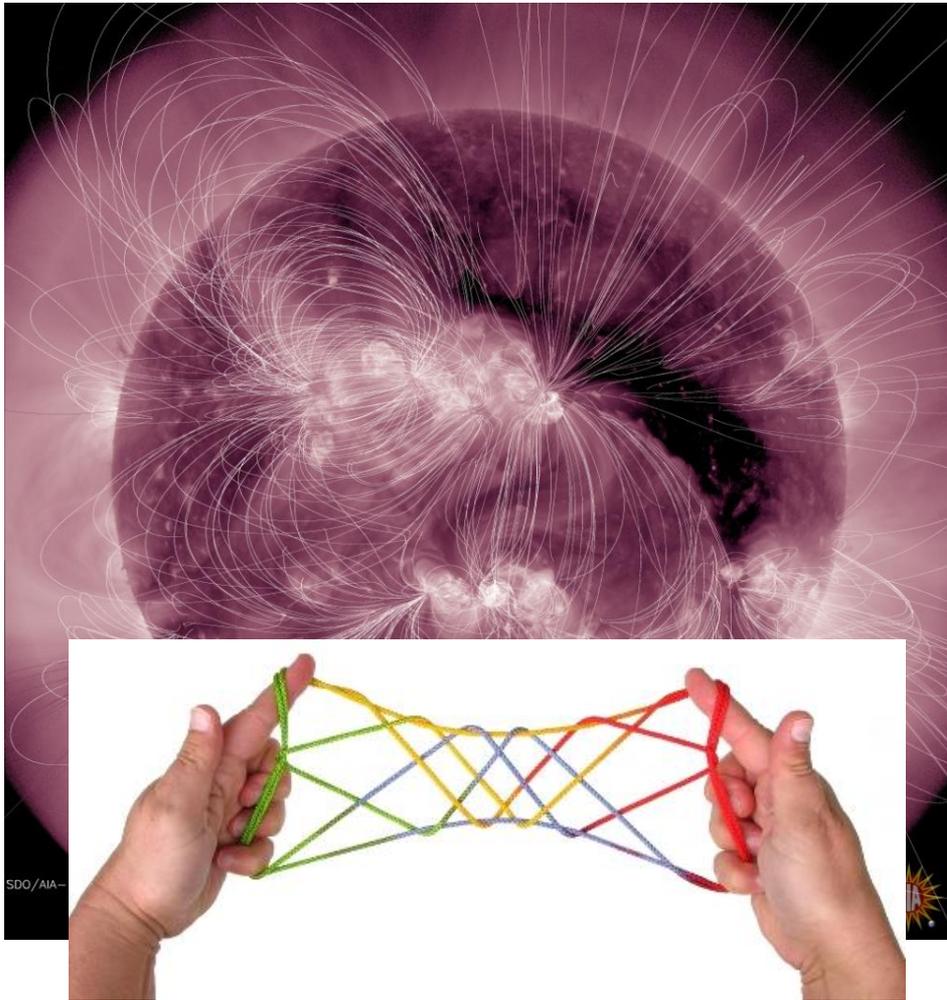


Short answer:  
magnetic field lines.

Plasma is frozen-in, and:

- In atmosphere:  
 $P_G/P_B \ll 1$ , **B** drives plasma
- Below the surface:  
 $P_G/P_B \gg 1$ , plasma drives **B**

# An unwrapping structure! but what exactly is “unwrapping”?



Short answer:  
magnetic field lines.

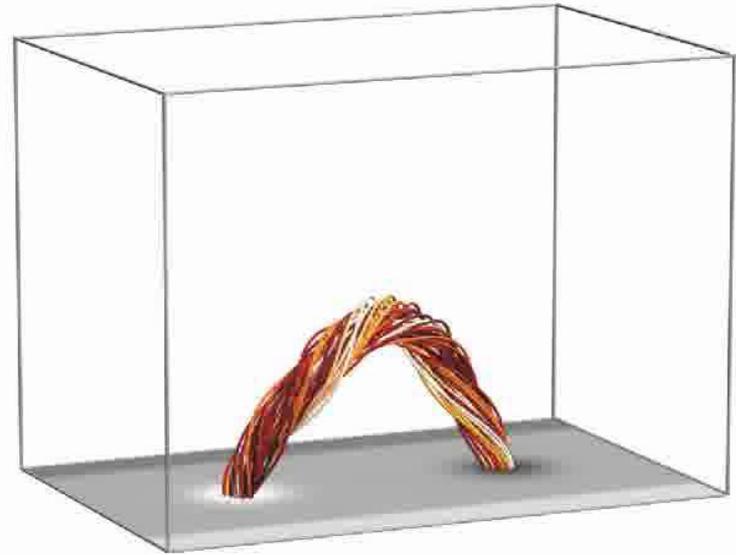
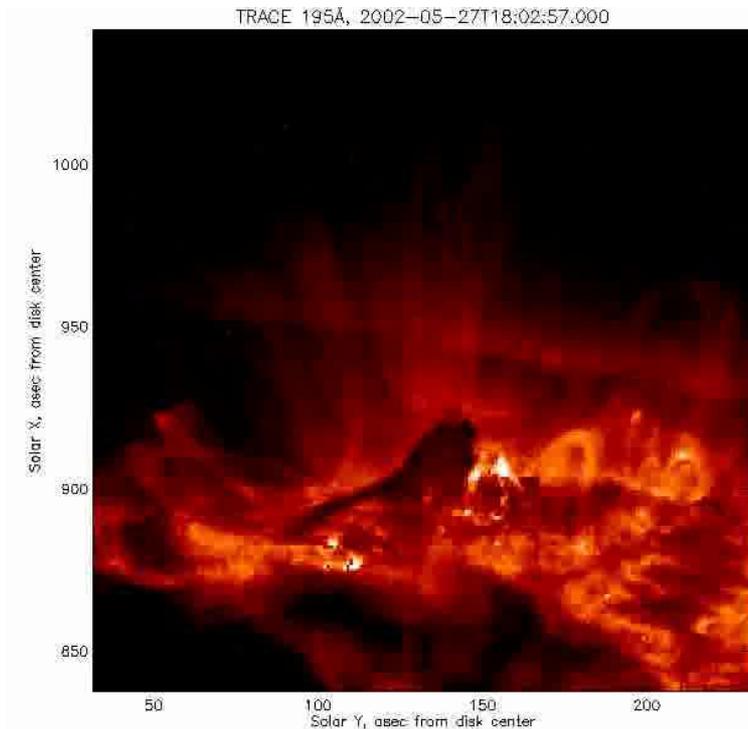
Plasma is frozen-in, and:

- In atmosphere:  
 $P_G/P_B \ll 1$ ,  $\mathbf{B}$  drives plasma
- Below the surface:  
 $P_G/P_B \gg 1$ , plasma drives  $\mathbf{B}$

Magnetic field lines in the atmosphere get entangled as their footpoints move around

# Consequences... solar eruptions!

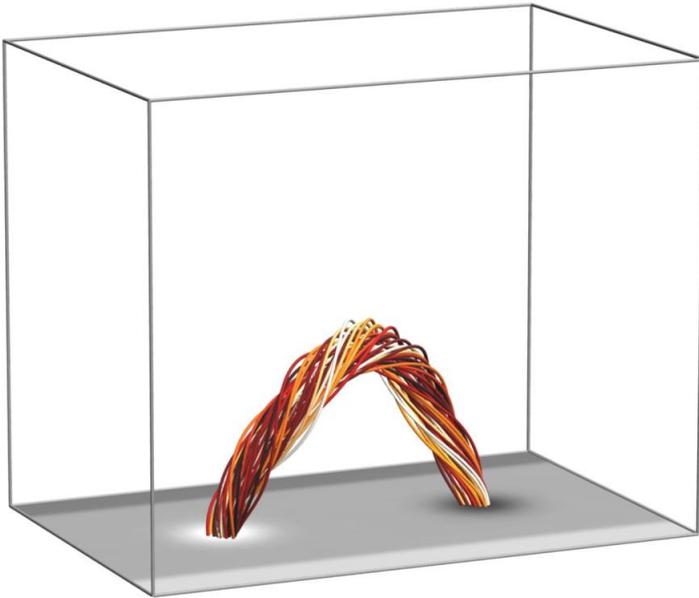
- A field too tangled may become unstable and explode
- Example: when *twisted* flux tube gets twisted beyond some critical value



# Twist in magnetic equilibria

---

Idealized case:

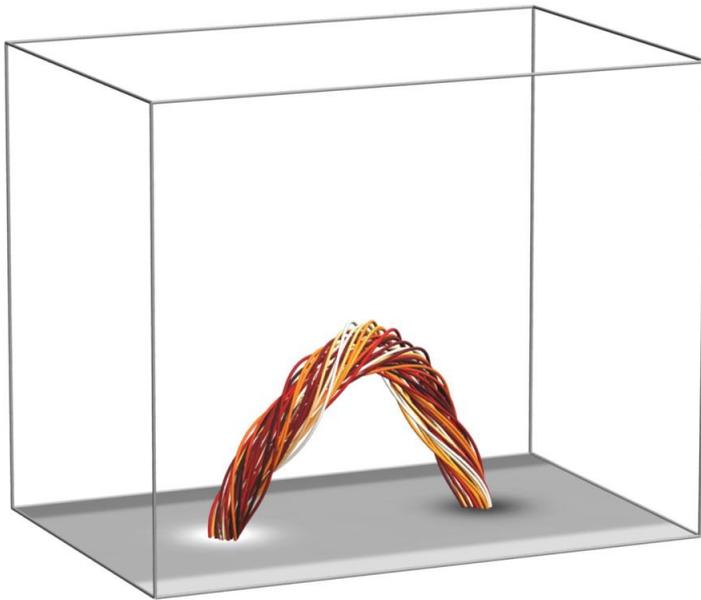


$T_w$ : total turns about the axis

# Twist in magnetic equilibria

---

Idealized case:



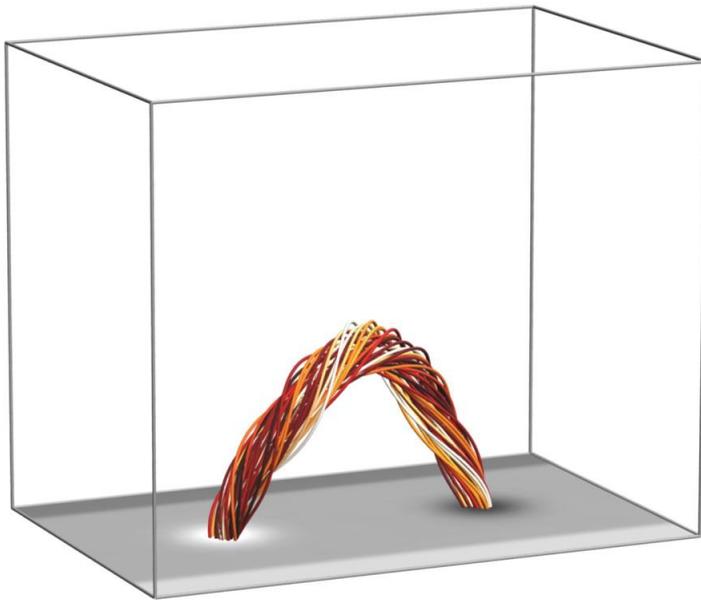
Tw: total turns about the axis  
“kink unstable” if  $Tw \geq 1.5$

Hood & Priest (1979)

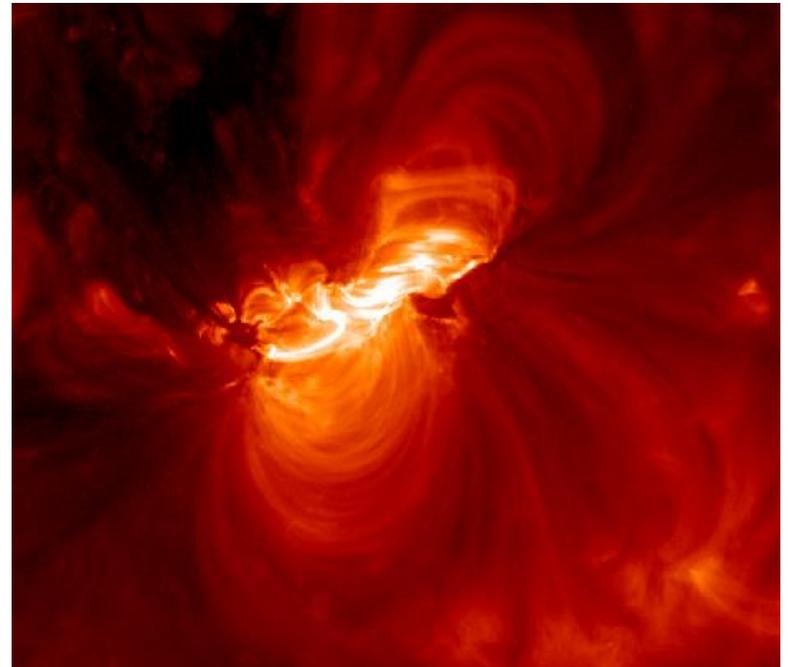
# Twist in magnetic equilibria

---

Idealized case:



*Actual observations:*



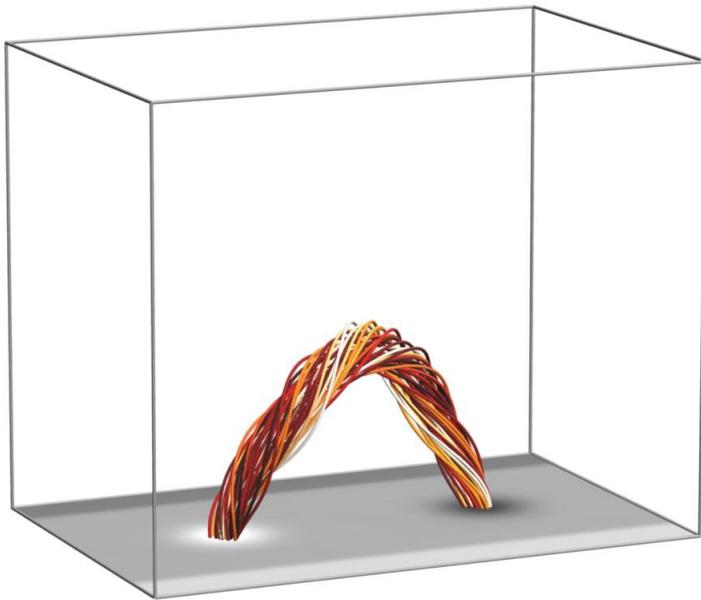
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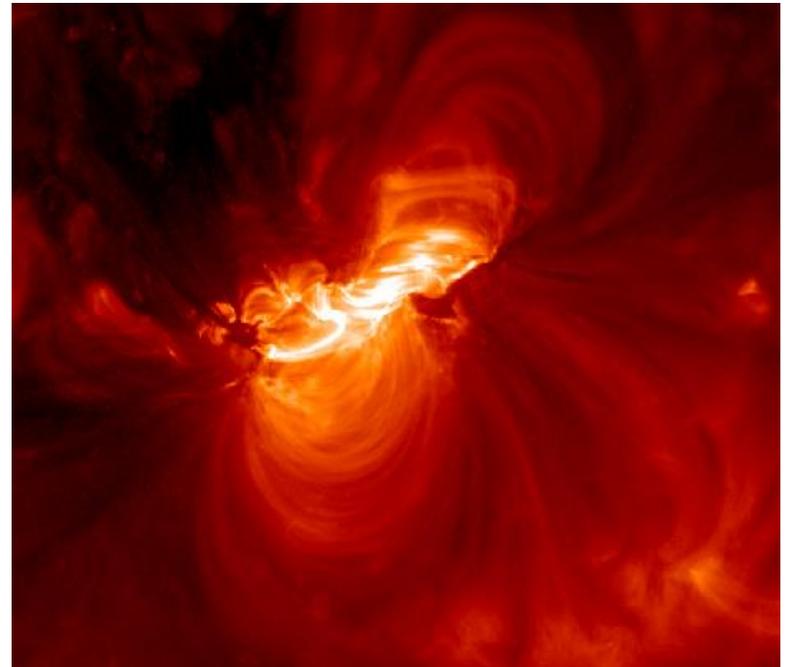
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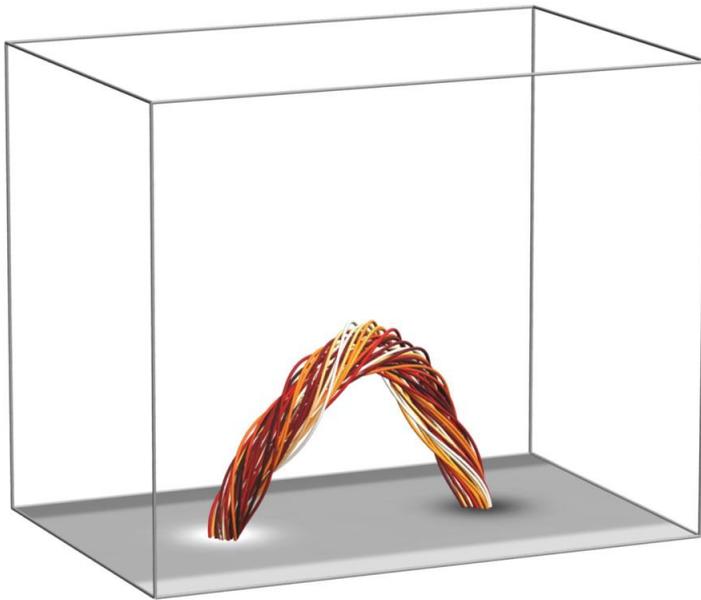


How to measure?

# Twist in magnetic equilibria

---

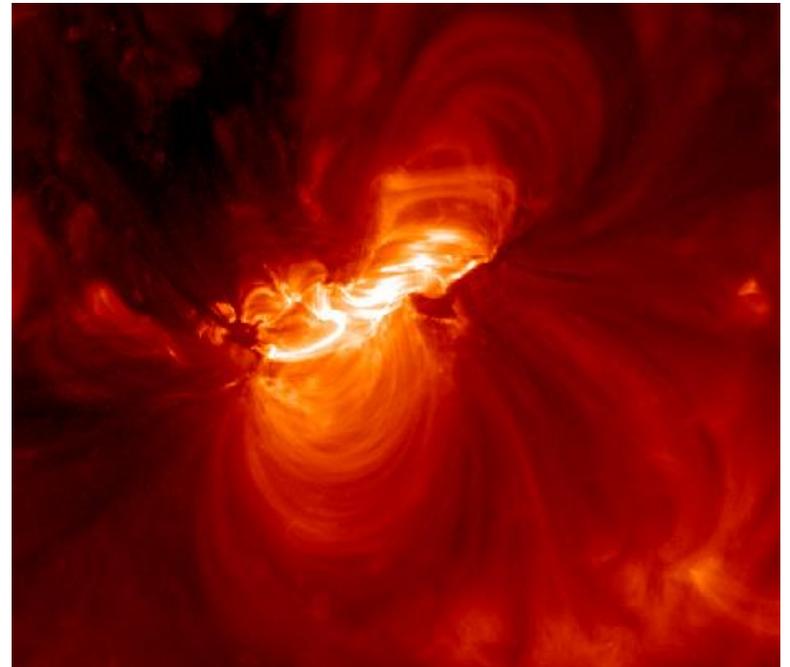
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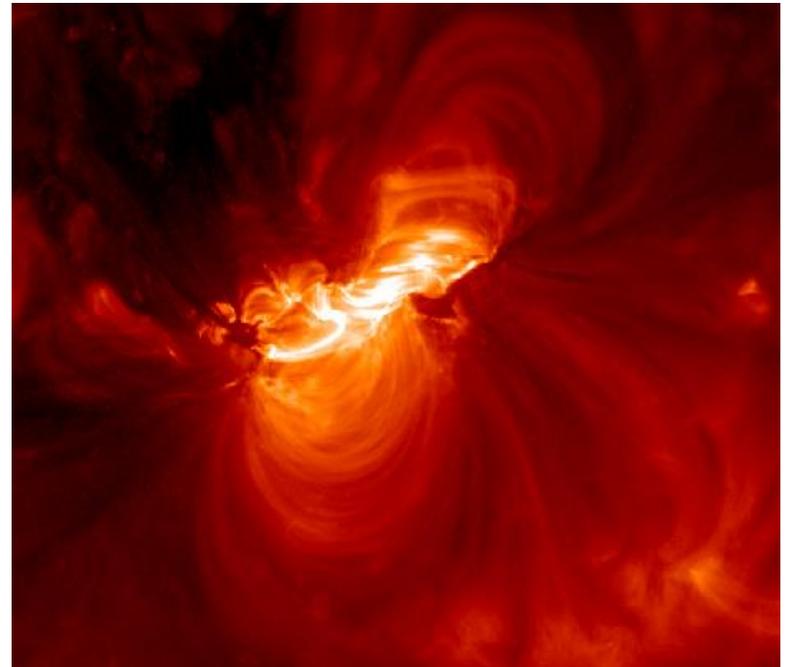
How to measure?  
*What* to measure?

# Twist in magnetic equilibria

---

Magnetic equilibrium  
in the corona:  $\mathbf{F}_L=0$

*Actual observations:*



How to measure?  
*What* to measure?

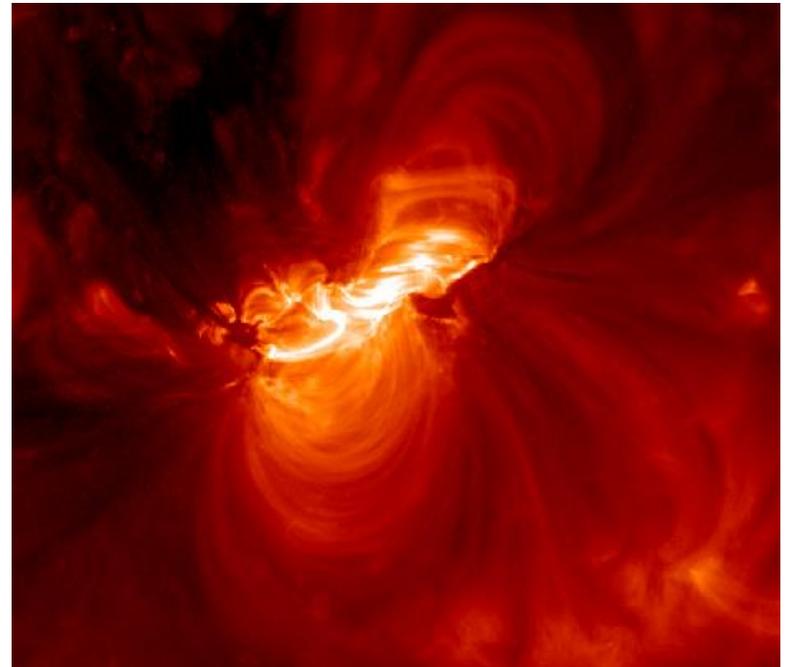
# Twist in magnetic equilibria

---

Magnetic equilibrium  
in the corona:  $\mathbf{F}_L=0$

or,  $\nabla \times \mathbf{B} = \alpha \mathbf{B}$ .

*Actual observations:*



How to measure?  
*What* to measure?

# Twist in magnetic equilibria

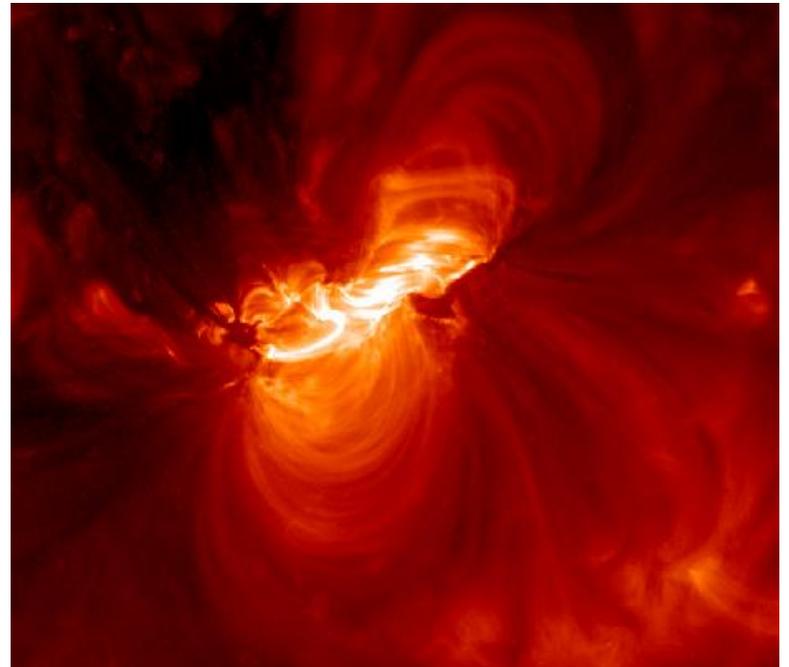
---

Magnetic equilibrium  
in the corona:  $\mathbf{F}_L=0$

or,  $\nabla \times \mathbf{B} = \alpha \mathbf{B}$ .

Force-free parameter  $\alpha$   
is closely related to twist!

*Actual observations:*

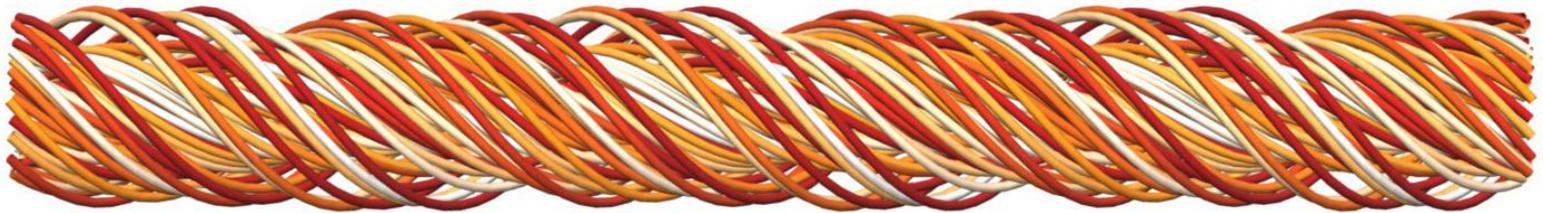


How to measure?  
*What* to measure?

# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$

---

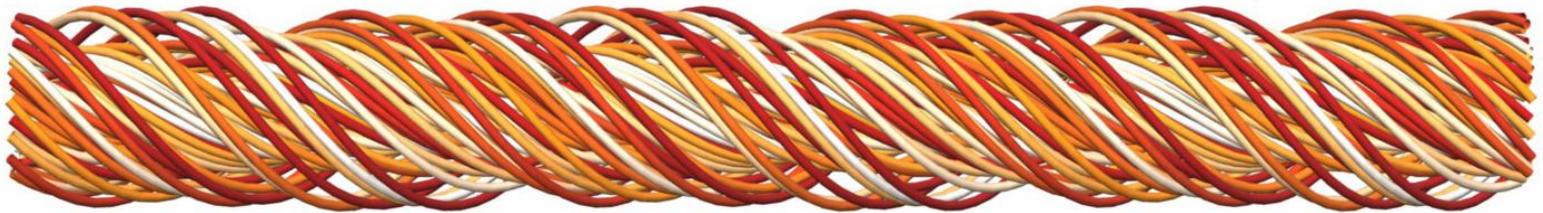
In a straight uniformly twisted flux tube,  
 $\alpha$  is angle per unit length.



# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$

---

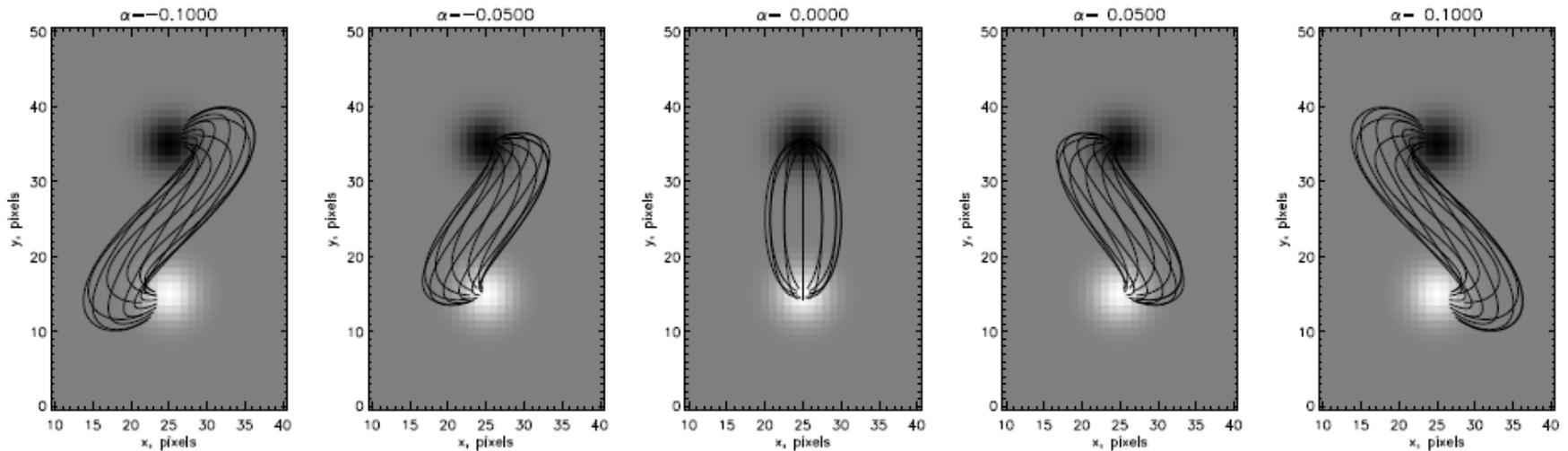
In a straight uniformly twisted flux tube,  
 $\alpha$  is angle per unit length.



In general,  $\alpha$  is still closely related to  
the shape of field lines.

# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$

Intuitive insight:  $\alpha$  is closely related to twist of field lines



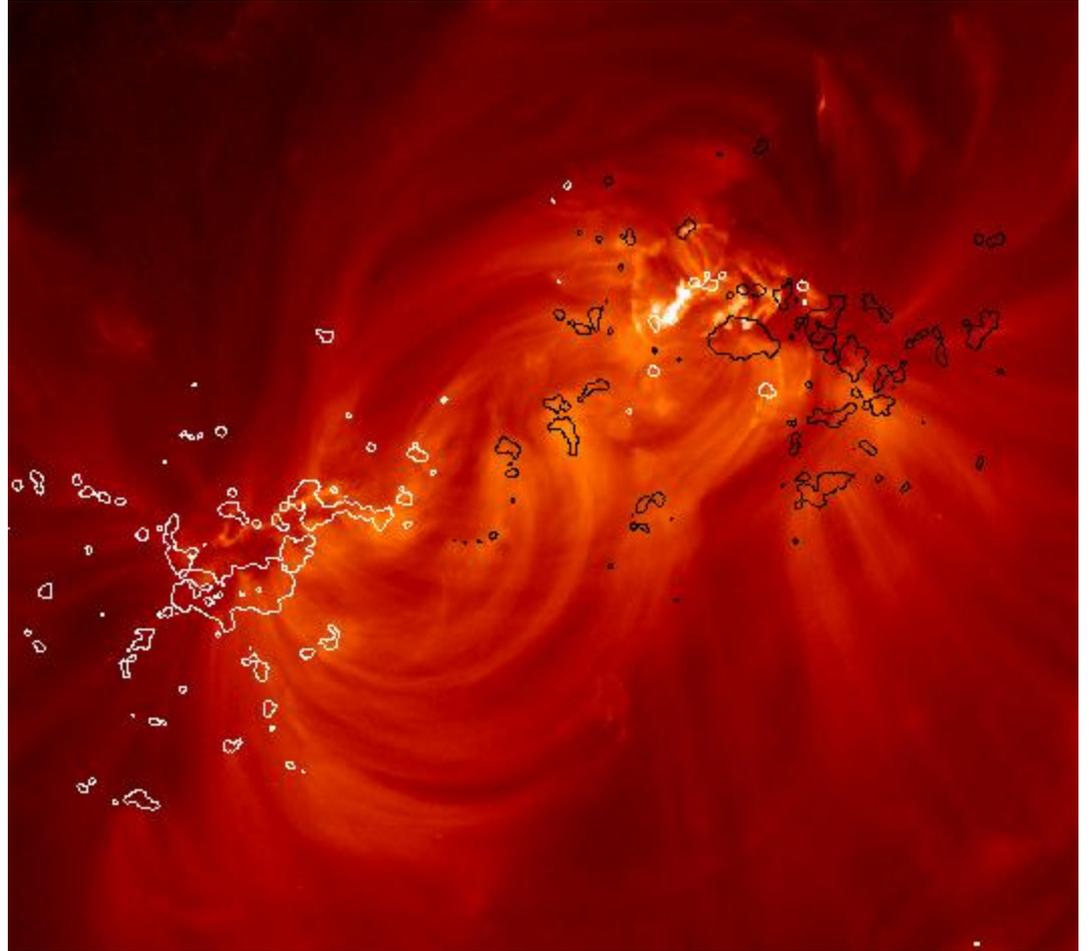
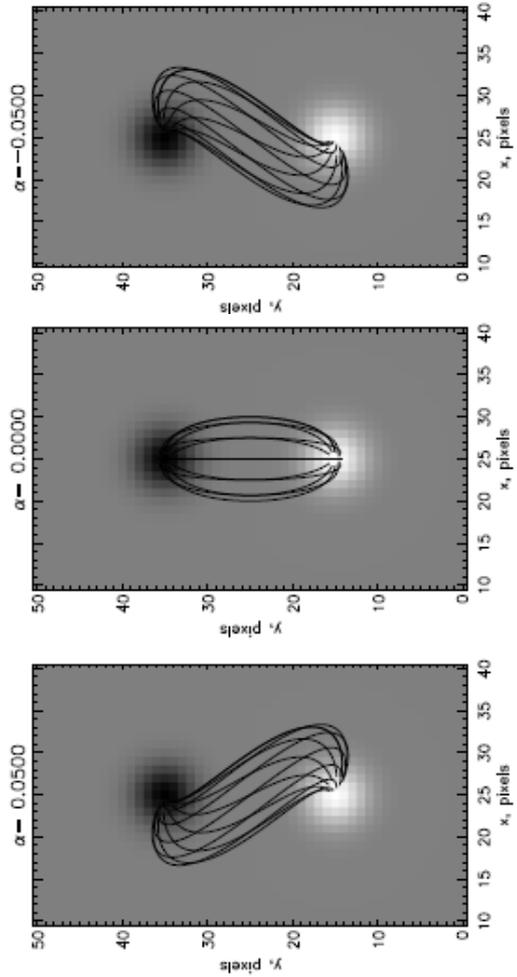
$\alpha < 0$

0

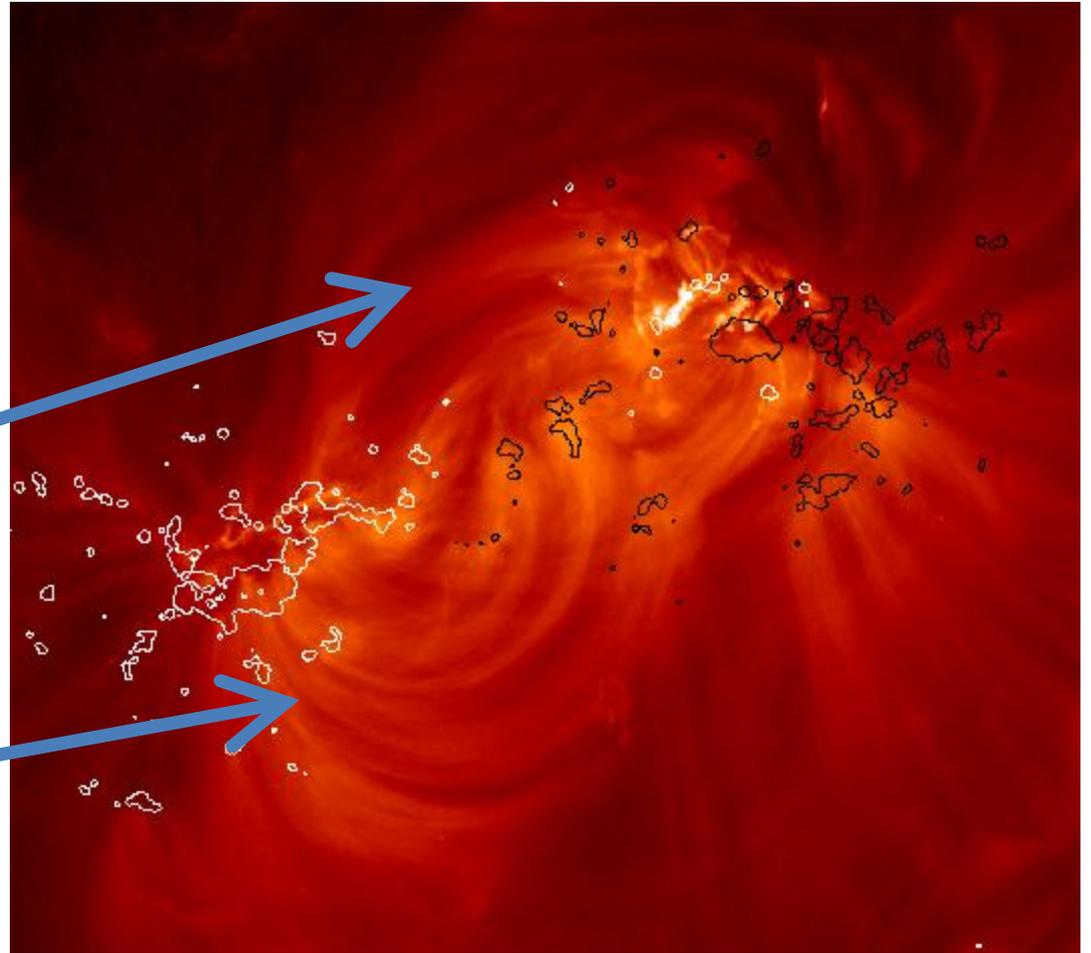
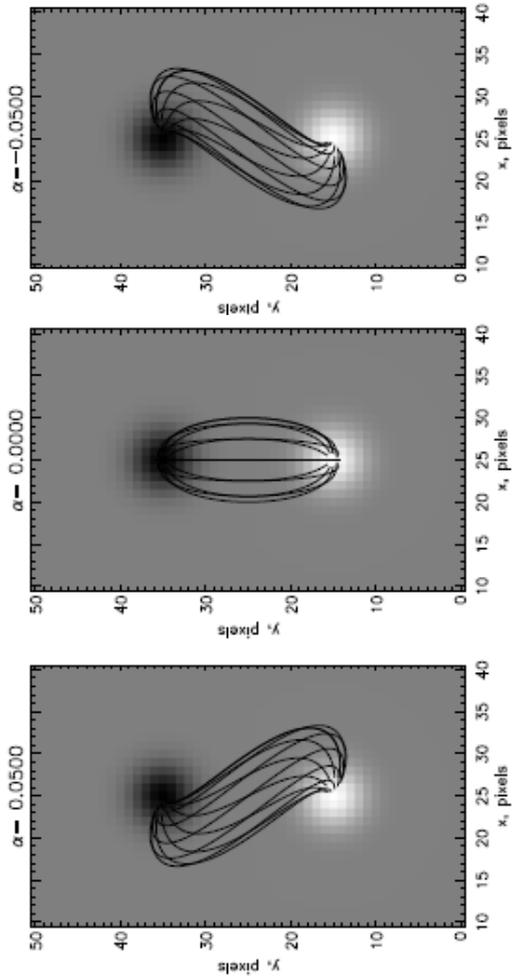
$\alpha > 0$

$\alpha$

# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$



# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$



# Force-free field: $\nabla \times \mathbf{B} = \alpha \mathbf{B}$

Const- $\alpha$  fields:

easy to calculate;

don't always work.

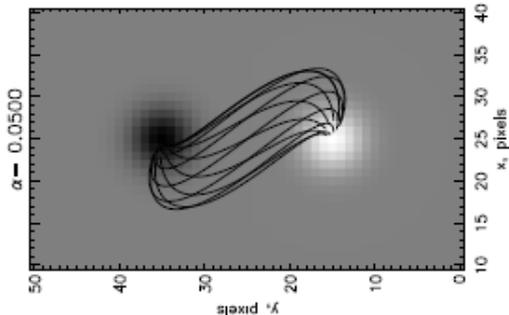
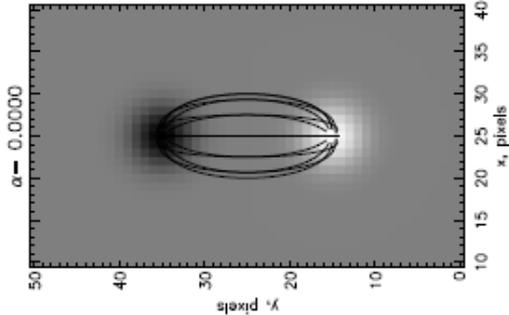
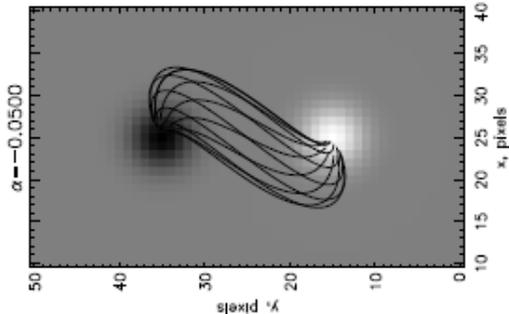
can't "combine" them

$$\nabla \times (\mathbf{B}_1 + \mathbf{B}_2) \neq \alpha (\mathbf{B}_1 + \mathbf{B}_2) \text{ if } \alpha_1 \neq \alpha_2.$$

In general, the equation

$$\nabla^2 \mathbf{B} + \alpha^2 \mathbf{B} = \mathbf{B} \times (\nabla \alpha)$$

is non-linear.



# Non-linear force-free field:

$$\nabla^2 \mathbf{B} + \alpha^2 \mathbf{B} = \mathbf{B} \times (\nabla \alpha)$$

Pros:

- Correct

Cons:

- Hard to solve
- Different methods give different answers
- B.C.: needs full  $\mathbf{B}$  at  $z=0$   
( $B_x$  and  $B_y$  are needed for getting  $\alpha$ )
- Have B.C. where the equations don't work!

(Demoulin et. al., 1971; DeRosa et. al., 2009)

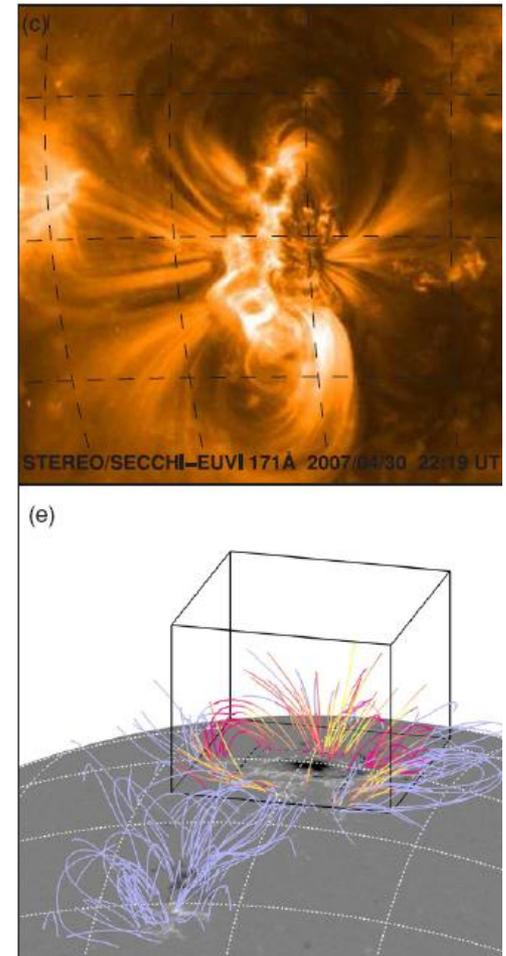


Fig. 1 from DeRosa et. al., 2009

# Non-linear force-free field:

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**BYPASS?**

(Demoulin et. al., 1971; DeRosa et. al., 2009)

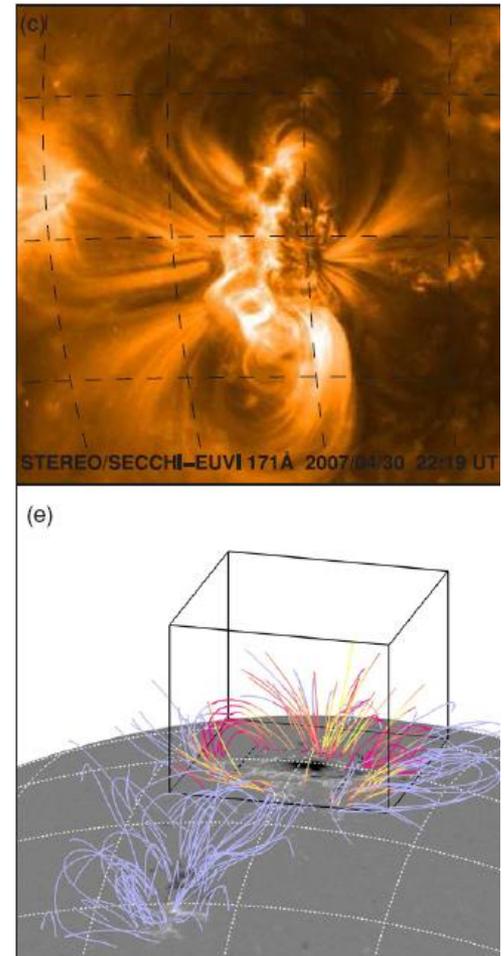


Fig. 1 from DeRosa et. al., 2009

# Non-linear force-free field:

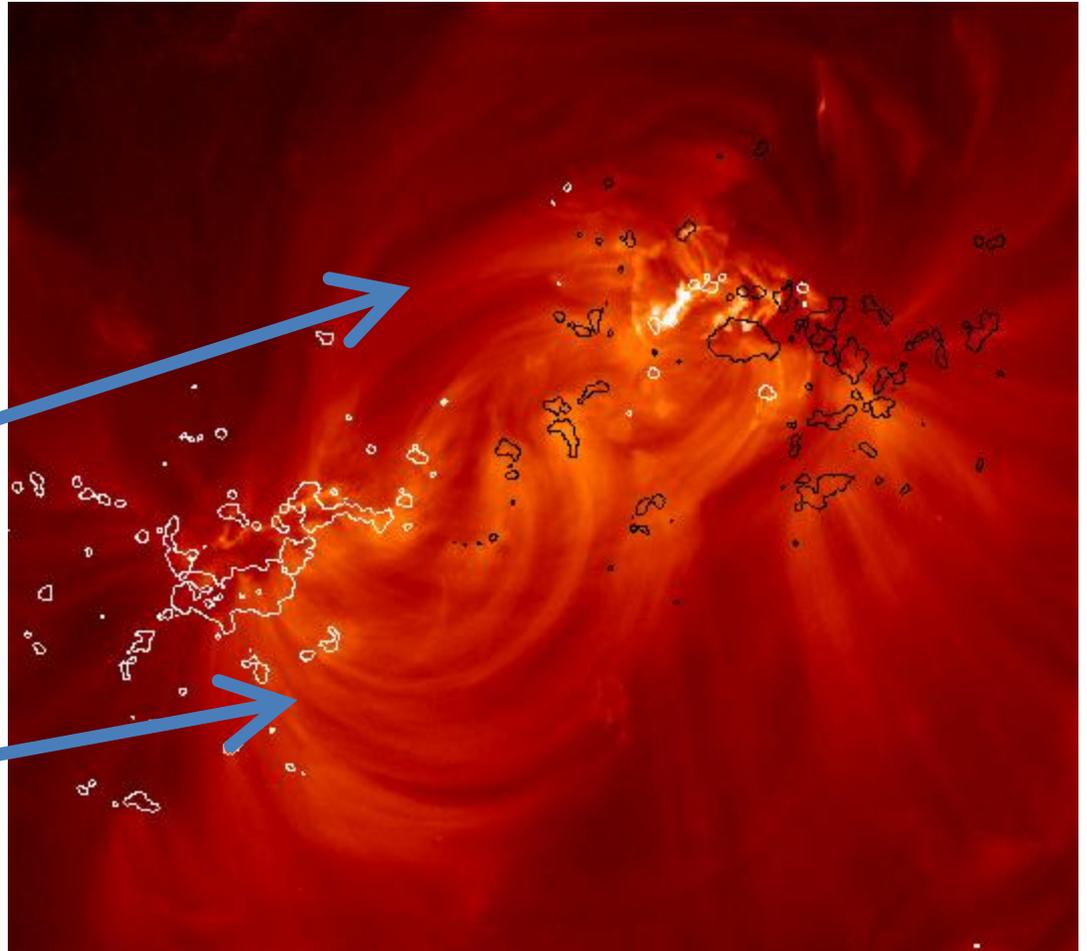
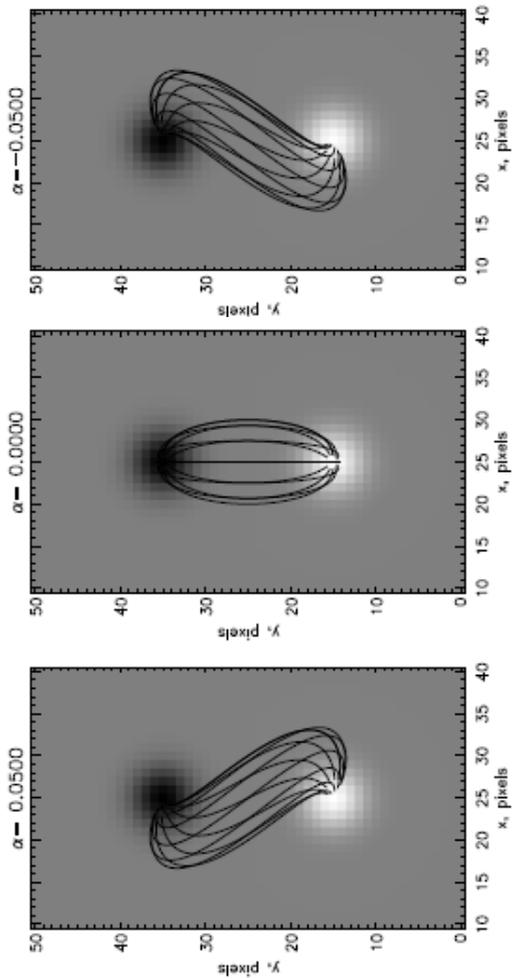
$$\nabla^2 \mathbf{B} + \alpha^2 \mathbf{B} = \mathbf{B} \times (\nabla \alpha)$$

---

We can bypass B.C. problem:

Use coronal images as extra constraints!

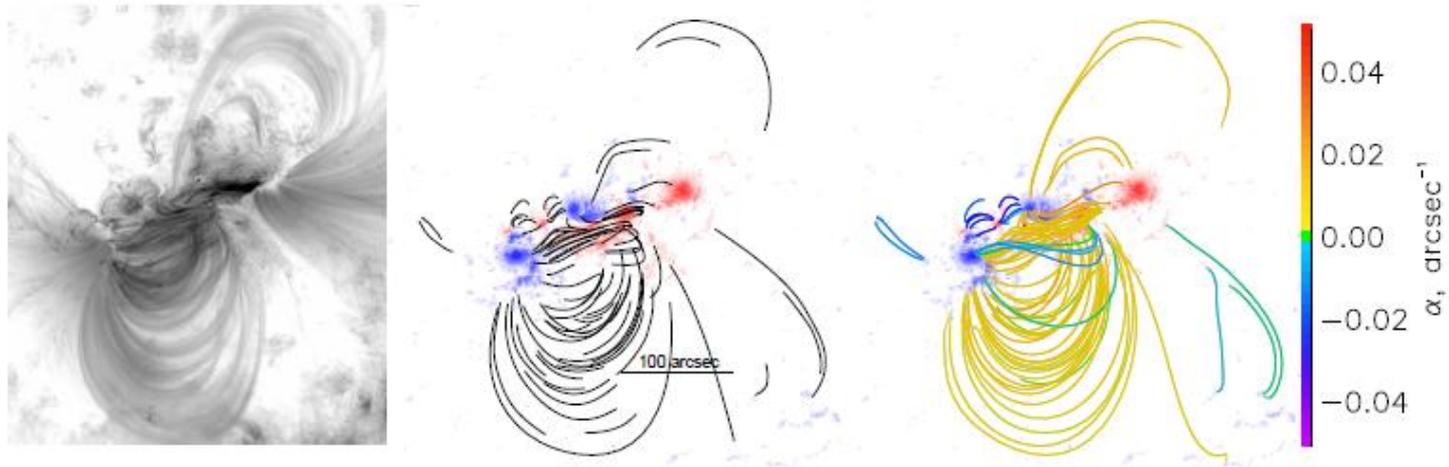
# Non-linear force-free field: using loops to understand the field structure!



# Non-linear force-free field: using loops to understand the field structure!

---

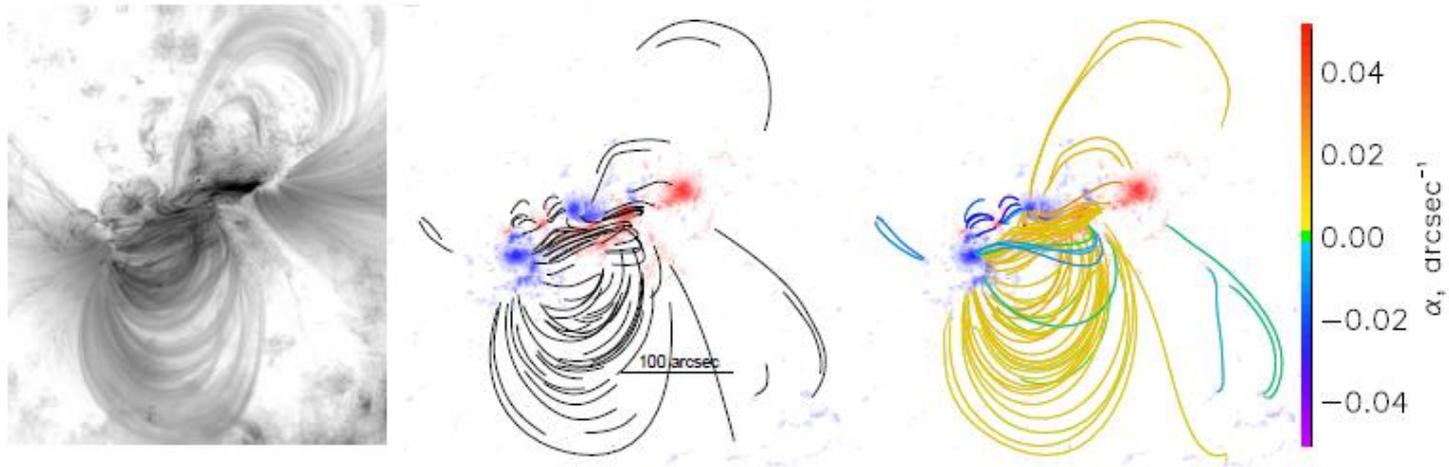
Step 1: convert images to “usable” data  
(by comparing to const- $\alpha$  fields  
to deduce  $\alpha$ 's and 3D paths of visible structures)



# Non-linear force-free field: using loops to understand the field structure!

---

Step 1: convert images to “usable” data  
(by comparing to const- $\alpha$  fields  
to deduce  $\alpha$ 's and 3D paths of visible structures)



Alternative: a plasma modeler (for example) might wish to model an equilibrium which has desired  $\alpha$ 's along the desired tracks!

# Non-linear force-free field: using loops to understand the field structure!

---

Step 2: use evaluated (or desired)  $\alpha$ 's and 3d trajectories and line-of-sight field component to solve the PDE.

*Basic idea: "give me a field which matches constraints in the volume as closely as possible, while satisfying a given PDE as closely as possible."*

# Non-linear force-free field: using loops to understand the field structure!

---

Step 2: use evaluated (or desired)  $\alpha$ 's and 3d trajectories and line-of-sight field component to solve the PDE.

*Basic idea: "give me a field which matches constraints in the volume as closely as possible, while satisfying a given PDE as closely as possible."*

Normal approach: PDE+(boundary conditions).

Hack: PDE+(constraints in the volume)!

possible use in other areas: a PDE, elliptic w.r.t. one variable and hyperbolic w.r.t. the other variable; hyperbolic initial state is poorly known at boundary but known on streamlines in the volume.

# Grad-Rubin Iteration

(1958)

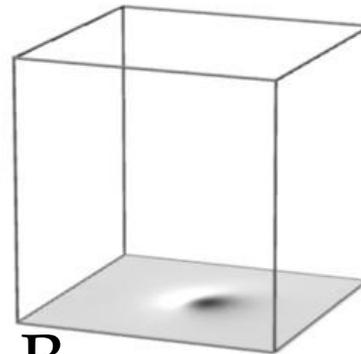
Problem:

$$\nabla \times \mathbf{B} = \alpha \mathbf{B}, \quad \mathbf{B} \cdot \nabla \alpha = 0$$

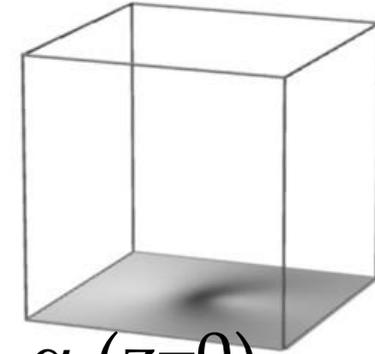
Iteration:

$$\begin{aligned} \mathbf{B}^{(0)} &\Rightarrow \mathbf{B}^{(0)} \cdot \nabla \alpha^{(0)} = 0 \\ \Rightarrow \nabla \times \mathbf{B}^{(1)} &= \alpha^{(0)} \mathbf{B}^{(0)} \\ \Rightarrow \mathbf{B}^{(1)} &\Rightarrow \alpha^{(1)} \Rightarrow \dots \end{aligned}$$

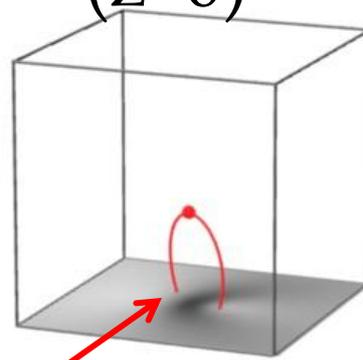
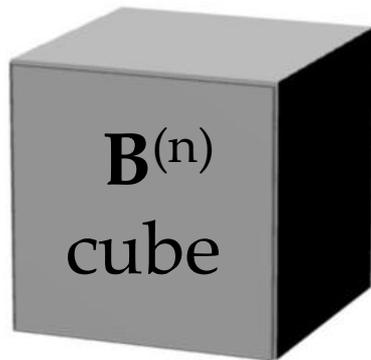
Initial data:



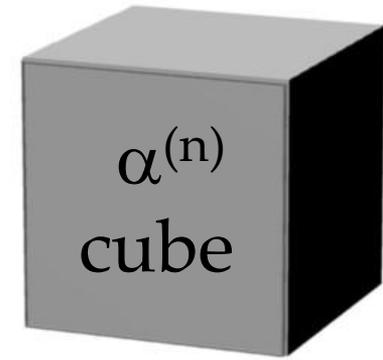
$B_z$   
( $z=0$ )



$\alpha$  ( $z=0$ )



Trace field line; assign  $\alpha$   
based on the footpoints



$$\nabla \times \mathbf{B}^{(n+1)} = \alpha^{(n)} \mathbf{B}^{(n)}$$



# Quasi Grad-Rubin Iteration

(general idea)

Problem:

$$\nabla \times \mathbf{B} = \alpha \mathbf{B}, \quad \mathbf{B} \cdot \nabla \alpha = 0$$

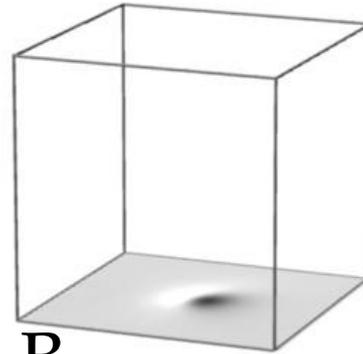
Iteration:

$$\mathbf{B}^{(0)} \Rightarrow \mathbf{B}^{(0)} \cdot \nabla \alpha^{(0)} = 0$$

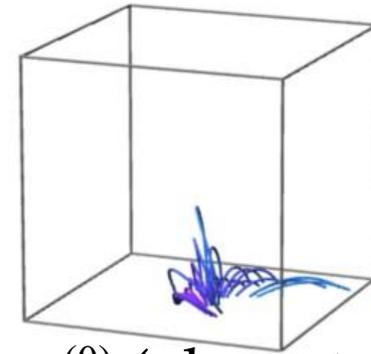
$$\Rightarrow \nabla \times \mathbf{B}^{(1)} = \alpha^{(0)} \mathbf{B}^{(0)}$$

$$\Rightarrow \mathbf{B}^{(1)} \Rightarrow \alpha^{(1)} \Rightarrow \dots$$

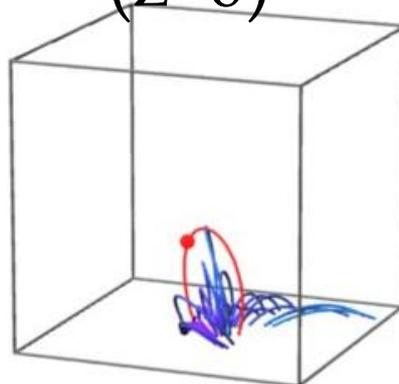
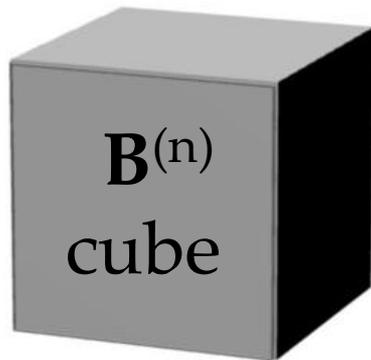
Initial data:



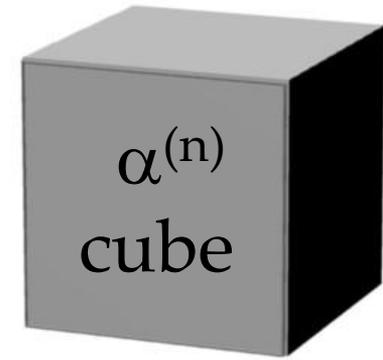
$B_z$   
( $z=0$ )



$\alpha^{(0)}$  (along trajectories)

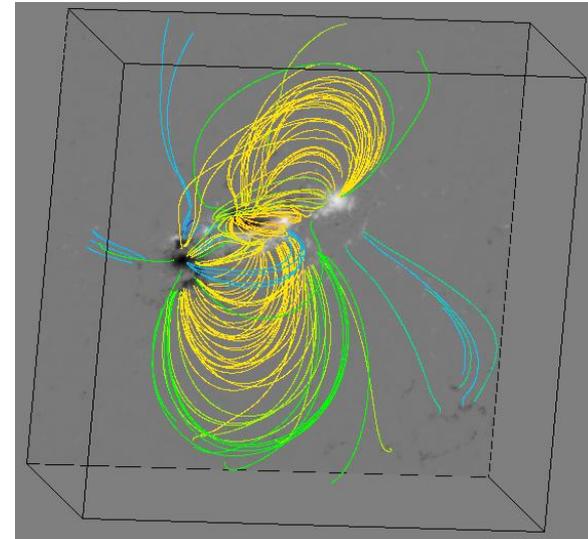
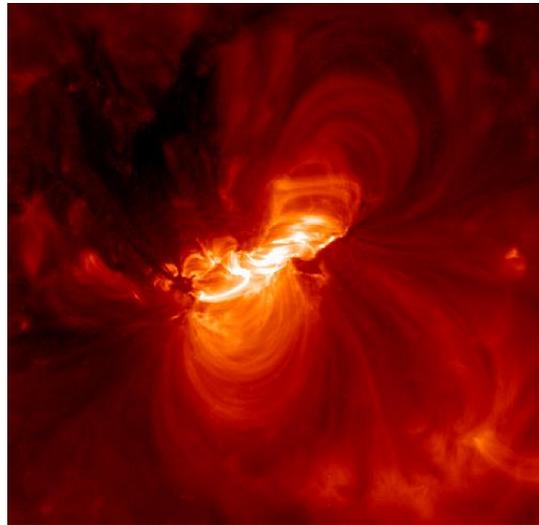


Trace field line; assign  $\alpha^{(n)}$   
based on the average  $\langle \alpha^{(n-1)} \rangle$



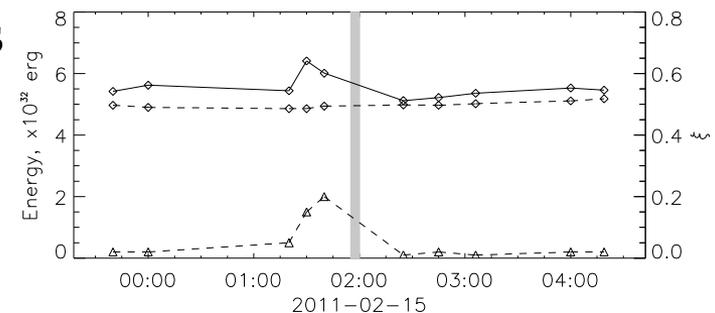
$$\nabla \times \mathbf{B}^{(n+1)} = \alpha^{(n)} \mathbf{B}^{(n)}$$

# Coronal images as guides for magnetic modeling: Quasi Grad-Rubin



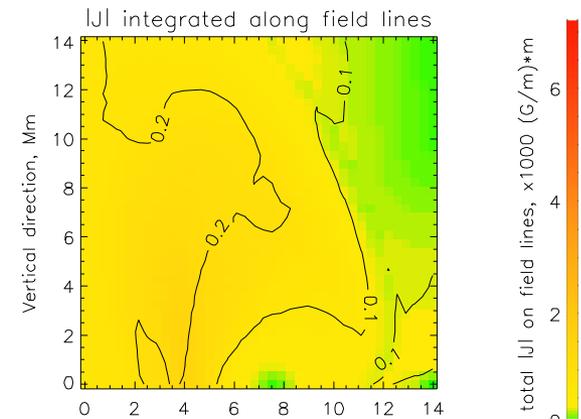
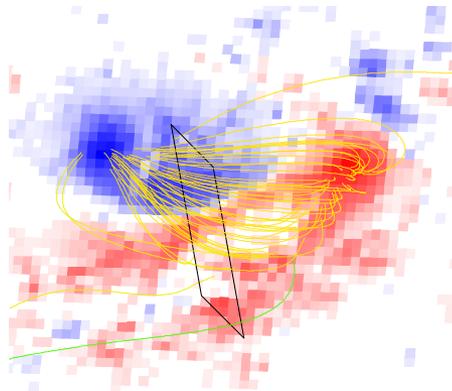
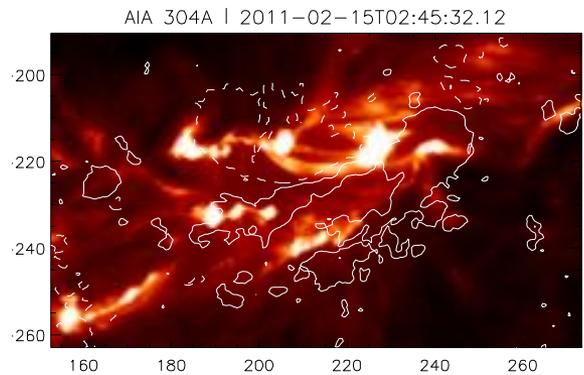
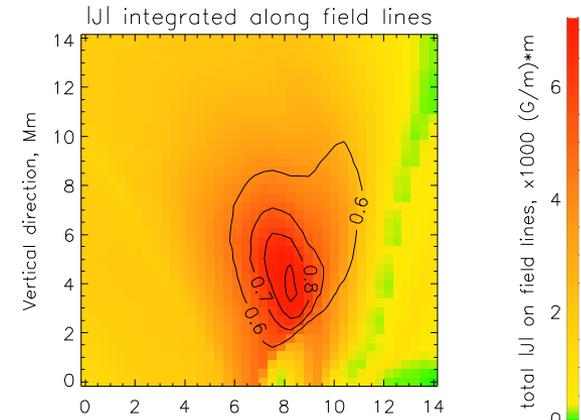
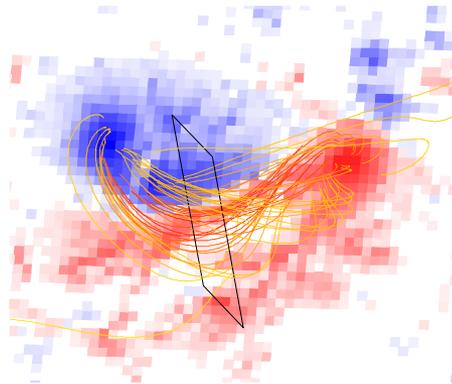
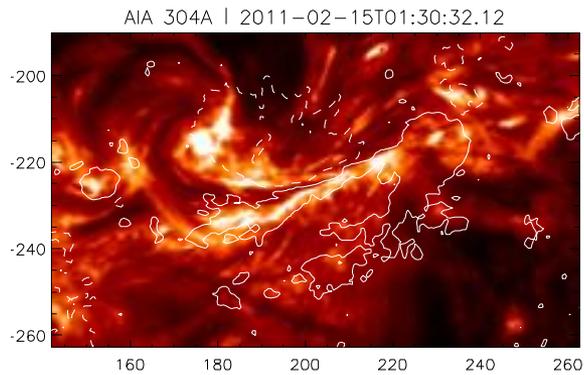
Key results:

- realistic representation of coronal features
- not very sensitive to choice of loops in quiescent and post-flare stages
- more sensitive in pre-flare stages
- a successful estimate of energy release



Malanushenko et al (2014)

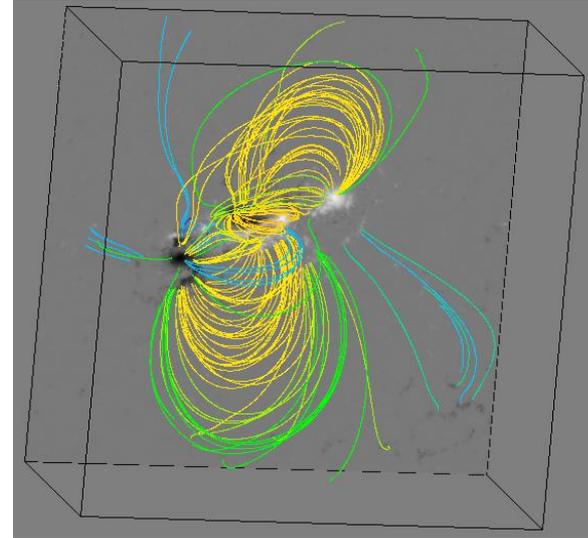
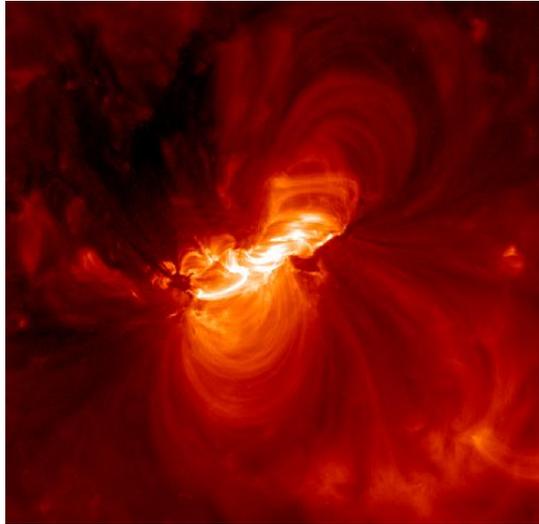
# Coronal images as guides for magnetic modeling



*QGR is a working tool for modeling the coronal magnetic field.*

# Using coronal images to understand solar eruptions

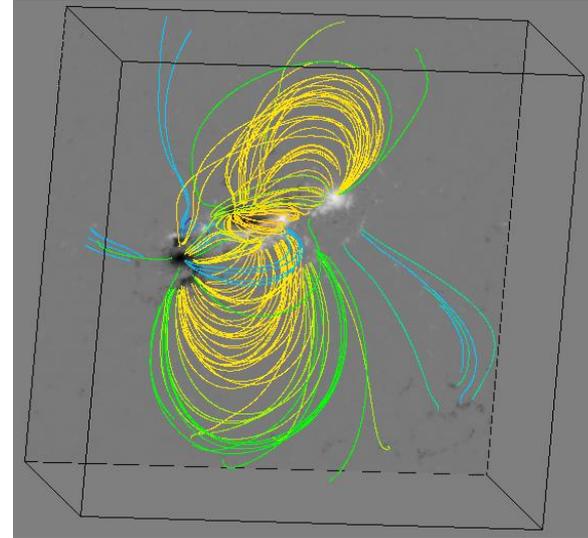
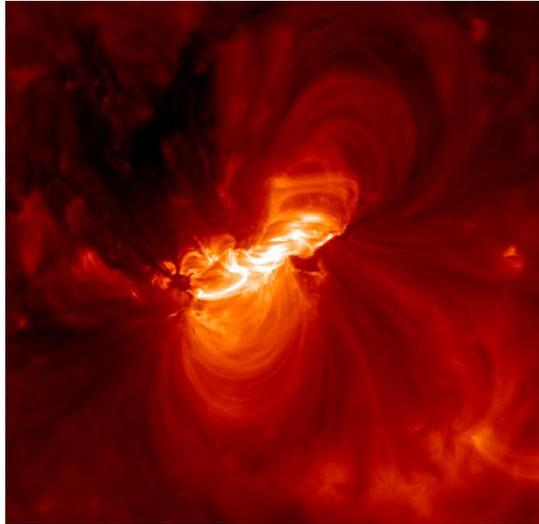
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Evolving a model of the *actually observed* and *actually erupted* structure in an MHD simulation.

# Using coronal images to understand solar eruptions

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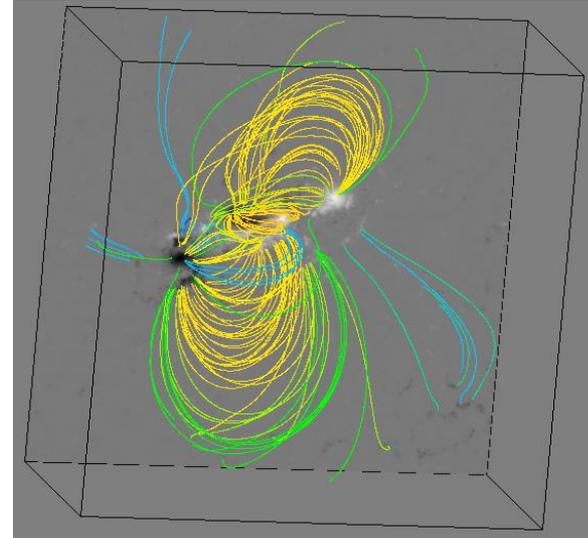
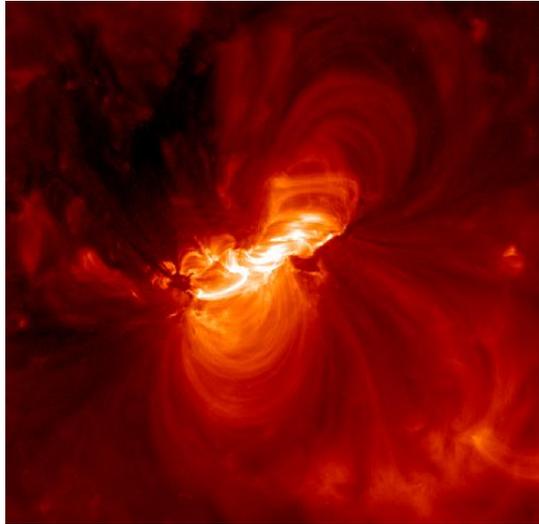
Evolving a model of the *actually observed* and *actually erupted* structure in an MHD simulation.

Results so far (preliminary)

- the structure appears to be stable
- the driving that was *thought* to make it erupt, makes it reconnect and relax but not erupt!

# Using coronal images to understand solar eruptions

---



Evolving a model of the *actually observed* and *actually erupted* structure in an MHD simulation.

Goal:

- understand what made it erupt in an *actually observed* way;
- provide a model of an observed CME for the space weather modeling.